

ECE 341 - Test #3

Markov Chains and Data Analysis

Open-Book, Open Notes. Calculators, Matlab, Tarot cards, Internet allowed. Just not other people.

Please sign if possible (i.e. you did not get help from someone else).

No aid given, received, or observed: _____

Due Monday, June 15th, 8am

Please make the subject "ECE 341 Test3" if submitting homework electronically to Jacob_Glower@yahoo.com (or on blackboard)

1) Markov Chains: Two people, A and B, are playing a game.

- A has a 60% chance of winning A gains +1 point on a win
- There is a 15% chance of a tie A loses one point on a tie
- A has a 25% chance of losing A loses two points on a loss

If A reaches +3 points, A wins the match

If A reaches -3 points, B wins the match

1a) What is the state transition matrix (going from k games to $k+1$ games)

1b) What is the chance that A will win the match assuming they start out at even (A has zero points)?

1c) What is the z-transform for the probability of A winning after k games?

1d) From the z-transforms, determine the probability of A winning the match

- i.e. the partial fraction expansion over the $(z-1)$ term

2) t-Test (One data set). A Monte-Carlo simulation was run 10 times. Each simulation dealt 10,000 hands for 5-card draw and counted the number of times you got a 3-of-a-kind.

hands = { 788 752 755 800 748 787 777 758 828 796 }

2a) If I run this experiment an 11th time, what number will I get with a confidence level of 90%? (5% tails)

2b) What is the 90% confidence interval for the actual probability of getting 3-of-a-kind with 5-card draw based upon this data?

3) t-Test (Two data sets): The average temperatures in March and November from 1942 - 2019 in Fargo, ND are:

(web site: http://www.bisonacademy.com/ECE111/Code/Fargo_Weather_Monthly_Avg.txt)

March = [33.8 17.6 20.2 35.1 34.7 24.7 17.7 22.1 20.7 15.7 20.4 28.0 25.5 16.8 19.5 27.5
30.9 30.9 15.5 34.5 22.7 29.0 20.8 13.7 29.7 26.8 34.0 15.2 18.6 27.6 23.9 36.0 22.9 18.4
22.9 32.0 23.5 20.4 20.7 33.5 22.9 29.8 23.4 32.8 31.6 31.4 29.5 20.0 31.4 30.3 32.6 25.6
30.5 28.3 17.3 20.1 26.5 31.1 35.2 22.9 20.0 24.7 30.3 28.0 27.4 31.6 22.8 24.0 35.4 20.5
41.6 17.3 22.3 33.5 38.3 29.5 26.2 19.8]

November = [27.5 29.6 32.9 26.0 27.1 22.2 29.1 34.1 22.3 21.0 30.8 35.1 34.5 18.8 30.5
28.9 29.7 20.5 29.9 30.1 35.0 34.7 29.2 26.0 23.1 29.0 31.0 30.5 27.8 29.6 28.5 25.1 29.2
31.1 23.2 25.6 22.7 24.5 33.0 35.4 24.1 31.2 29.7 15.4 23.1 33.4 27.5 24.0 32.1 22.0 27.3
26.6 34.0 21.2 17.7 23.2 29.3 37.1 25.9 39.7 27.9 24.9 34.2 31.2 31.9 31.1 31.7 38.4 29.2
33.8 30.3 28.2 22.8 36.2 41.8 28.3 22.4 22.0]

3a) What is the probability that March 2021 will be warmer than November 2021?

3b) What is the probability that March is warmer than November?

4) Chi-Squared Test: The following Matlab code generated 100 random values for X:

```
X = [];  
for i=1:100  
    X(i) = sum(-5*log(1 - rand(3,1)));  
end
```

It is conjectured that X has an exponential distribution with a mean of 15

$$f(x) = \left(\frac{1}{15}\right) e^{-t/15} u(t)$$

4a) Generate 100 values for X and give the sorted results (Matlab command *sort(X)*)

4b) Determine if X does or does not have this exponential pdf using a Chi-squared test.

5) F-Test (Three data sets): The average temperature in Fargo since 1942 in the months of June and July are:

http://www.bisonacademy.com/ECE111/Code/Fargo_Weather_Monthly_Avg.txt)

June = [62.6 63.7 65.5 60.3 64.7 61.4 63.8 65.6 65.5 60.7 67.3 64.9 65.3 65.4 70.7 62.7 59.7 68.1 63.3 68.6 66.2 68.8 67.2 63.9 66.1 62.6 64.1 57.3 67.8 67.4 66.9 64.7 64.4 65.2 68.5 66.5 64.7 65.4 65.7 62.8 59.1 66.0 65.7 60.0 67.5 69.1 73.8 64.1 66.9 70.1 61.9 63.1 68.2 71.4 67.0 68.9 63.4 66.3 62.7 65.9 69.0 65.4 62.5 68.2 68.5 69.8 63.6 63.6 66.5 66.8 69.9 67.5 67.2 67.1 68.8 67.8 70.3 67.1]

July = [68.8 73.0 69.3 68.6 71.2 71.5 71.2 71.3 67.9 68.5 69.7 69.9 71.8 74.5 68.0 75.3 67.3 72.2 71.4 70.4 68.8 73.6 74.0 68.5 73.8 67.9 69.6 68.3 71.8 65.0 68.3 68.2 73.6 74.2 71.7 72.2 69.5 71.9 71.8 71.1 70.9 73.5 70.6 68.9 71.5 74.0 75.8 75.8 70.0 70.2 64.3 67.0 67.6 70.0 67.8 69.2 71.7 71.5 70.6 72.5 73.0 70.4 68.2 71.3 74.9 74.0 70.3 66.5 72.0 74.5 76.6 71.7 69.4 72.5 71.9 72.1 70.9 72.2]

5a) What is the probability that the variance of June is different than the variance of July?

5b) What is the probability that

- June 1942 - 1967 (first 26 data points)
- June 1968 - 1993 (next 26 data points)
- June 1994 - 2019 (last 26 data points)

all have the same average temperature using an ANOVA test?