
Analog Computers

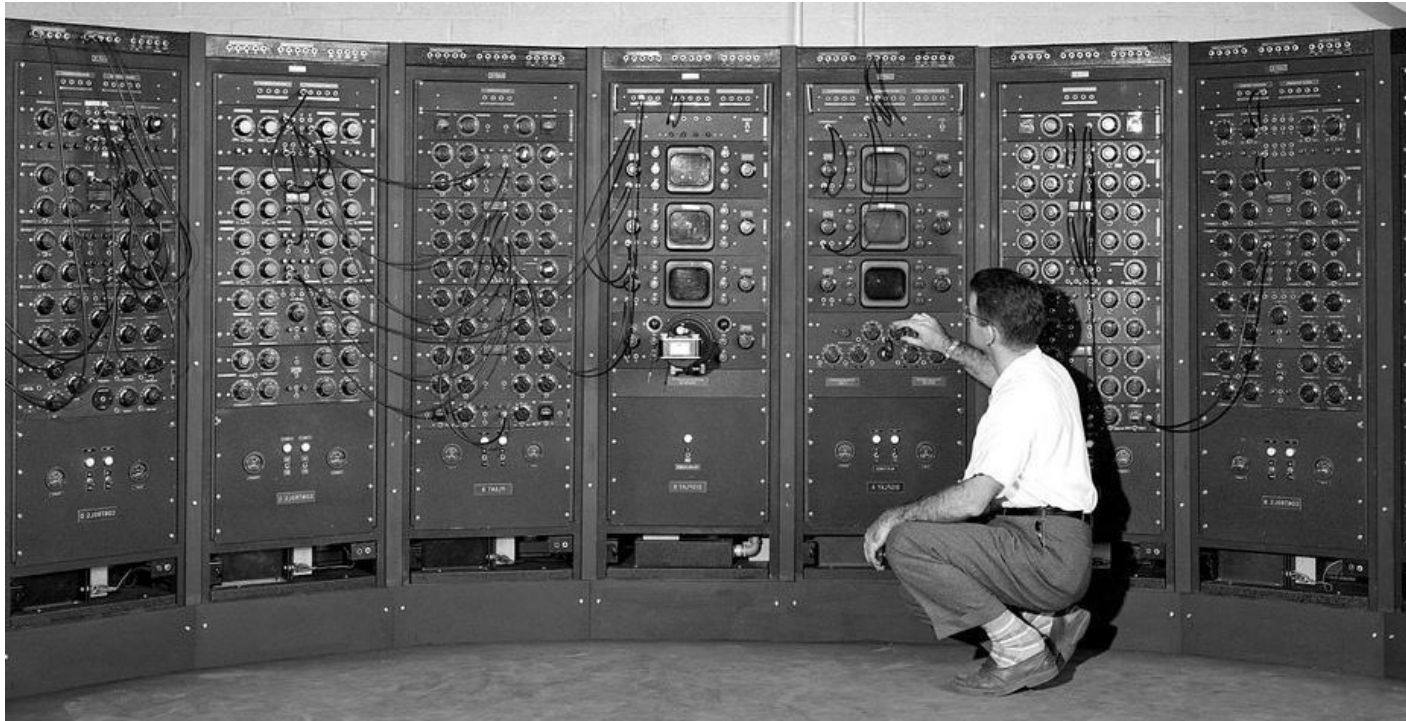
ECE 321: Electronics II

Lecture #11

Please visit [Bison Academy](#) for corresponding lecture notes, homework sets, and solutions

Analog Computers

- Electric circuit to implement a differential equation
- Allows you to duplicate the dynamics of an expensive system using an inexpensive circuit



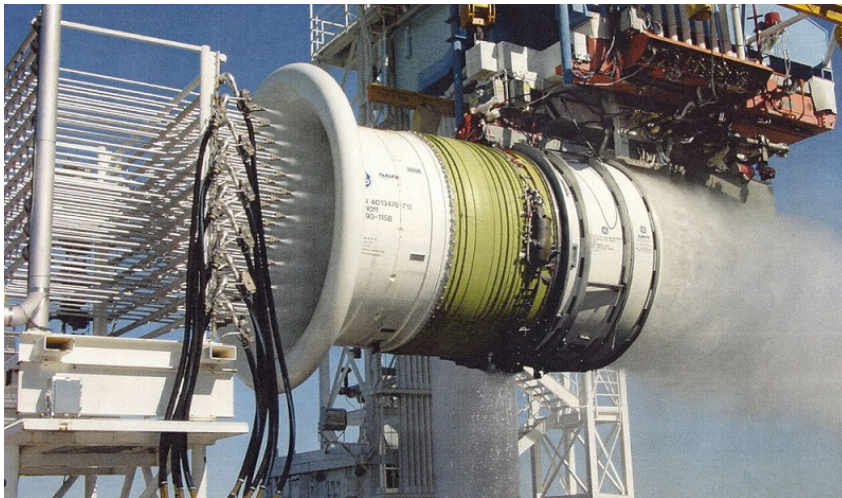
<https://images.easytechjunkie.com/1949-electronic-analog-computer.jpg>

Analog Computer Application

Jet Engine

<https://www.airlinerratings.com/did-you-know/how-is-a-jet-engine-tested/>

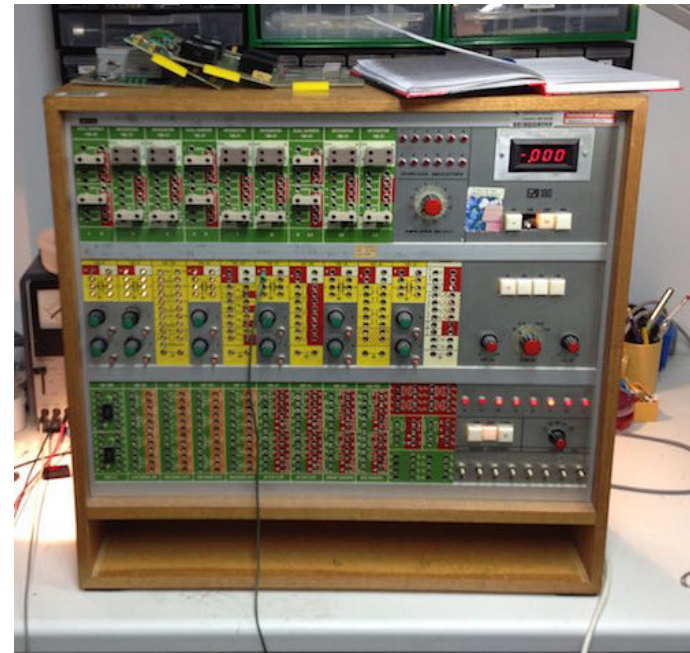
- \$10,000 / minute to test
- \$4,000,000 if you go unstable



Analog Computer

http://www.analogmuseum.org/english/collection/eai/180/1_small.jpg

- 10 cents / kWh to operated
- Red LED turns on if you go unstable



Analog Computers

Design a circuit to implement a generic proper transfer function

$$Y = \left(\frac{b_{n-1}s^{n-1} + b_{n-2}s^{n-2} + \dots + b_1s + b_0}{s^n + a_{n-1}s^{n-1} + a_{n-2}s^{n-2} + \dots + a_1s + a_0} \right) U$$

Solution:

There are many. This is one way to do it. Just to make it more manageable, assume a 3rd-order system

$$Y = \left(\frac{b_2s^2 + b_1s + b_0}{s^3 + a_2s^2 + a_1s + a_0} \right) U$$

Step 1: Change the problem. Create a dummy state, X

$$X = \left(\frac{1}{s^3 + a_2 s^2 + a_1 s + a_0} \right) U$$

$$Y = (b_2 s^2 + b_1 s + b_0) X$$

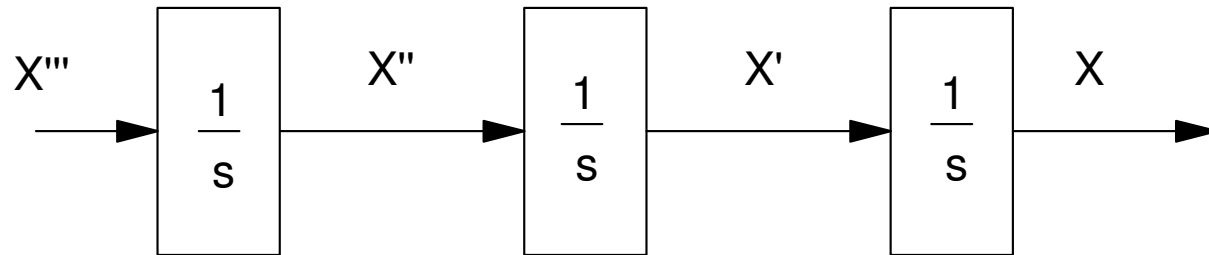
Step 2: Cross multiply and solve for the highest derivative of X :

$$X = \left(\frac{1}{s^3 + a_2 s^2 + a_1 s + a_0} \right) U$$

$$(s^3 + a_2 s^2 + a_1 s + a_0) X = U$$

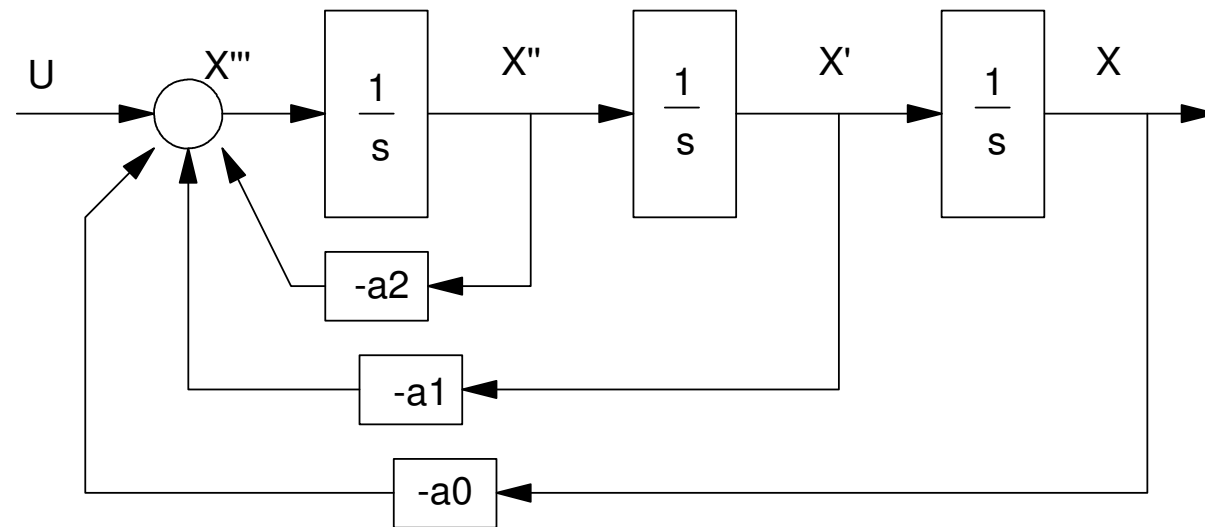
$$s^3 X = -(a_2 s^2 + a_1 s + a_0) X + U$$

Step 3: Given $s^n X$, solve for X by integrating n times (notation: X' means dx/dt)



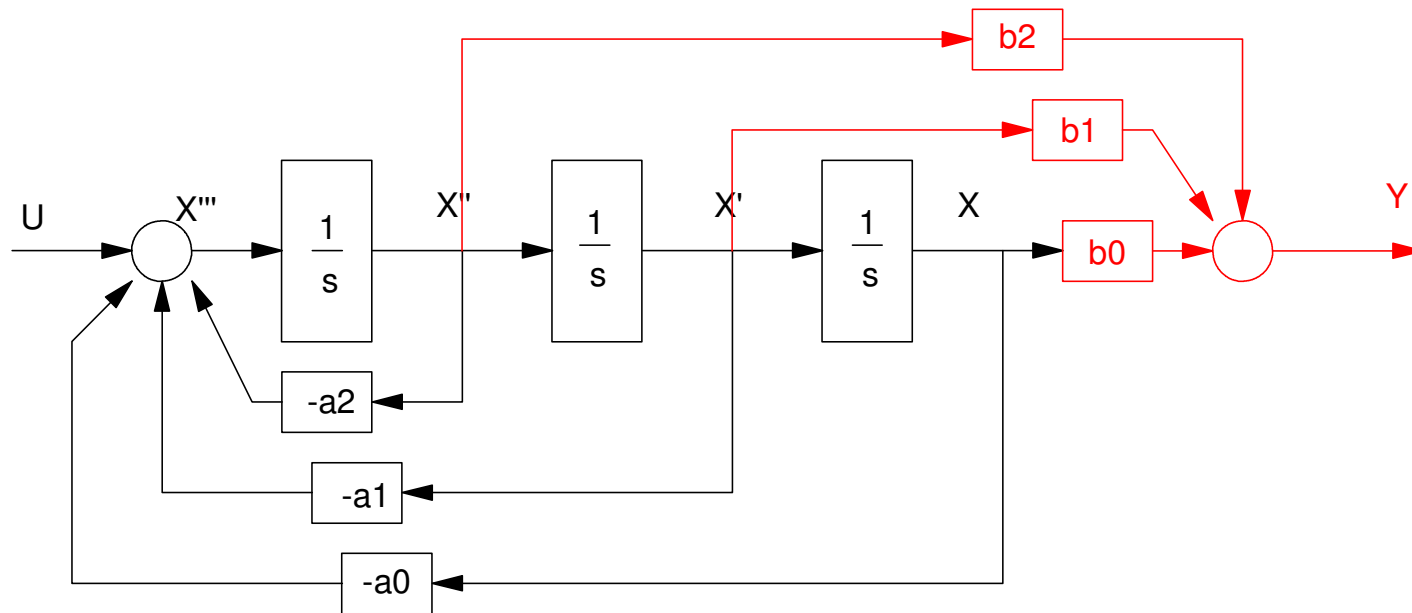
Step 4: Create X''' using the differential equation from step 2:

$$s^3 X = -(a_2 s^2 + a_1 s + a_0) X + U$$

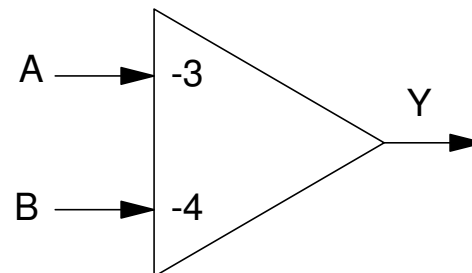


Step 5: Now that you know X and its derivatives, create Y :

$$Y = (b_2s^2 + b_1s + b_0)X$$

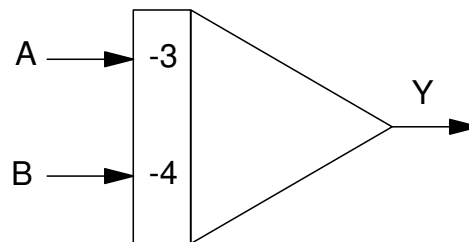


Step 6) Convert to analog computer notation. Here, a triangle means an amplifier:



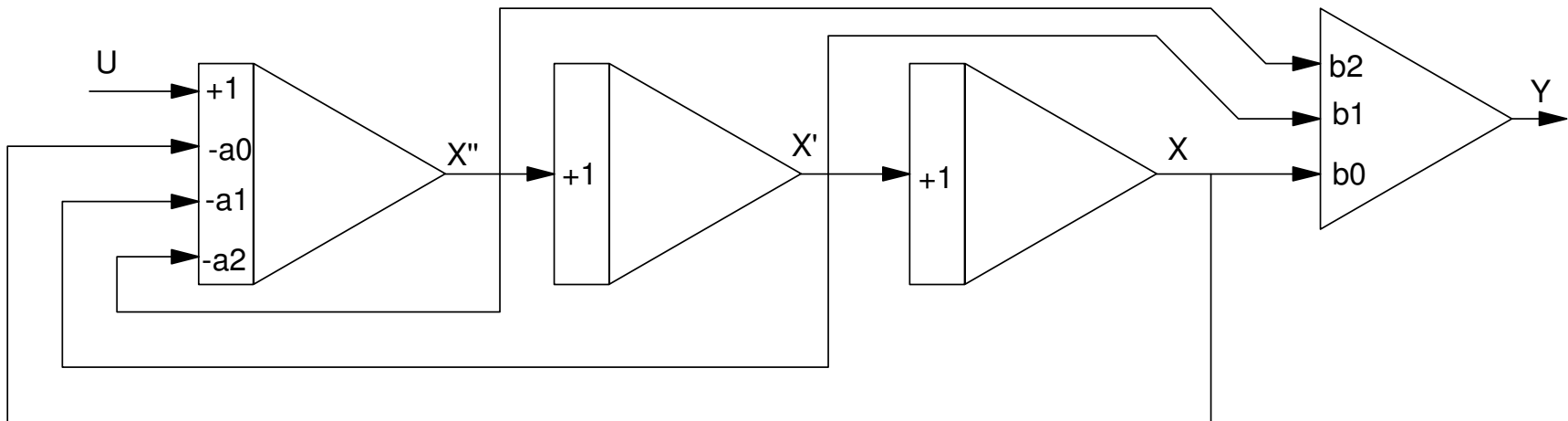
$$Y = -3A - 4B$$

whereas a triangle with a box means integrator:



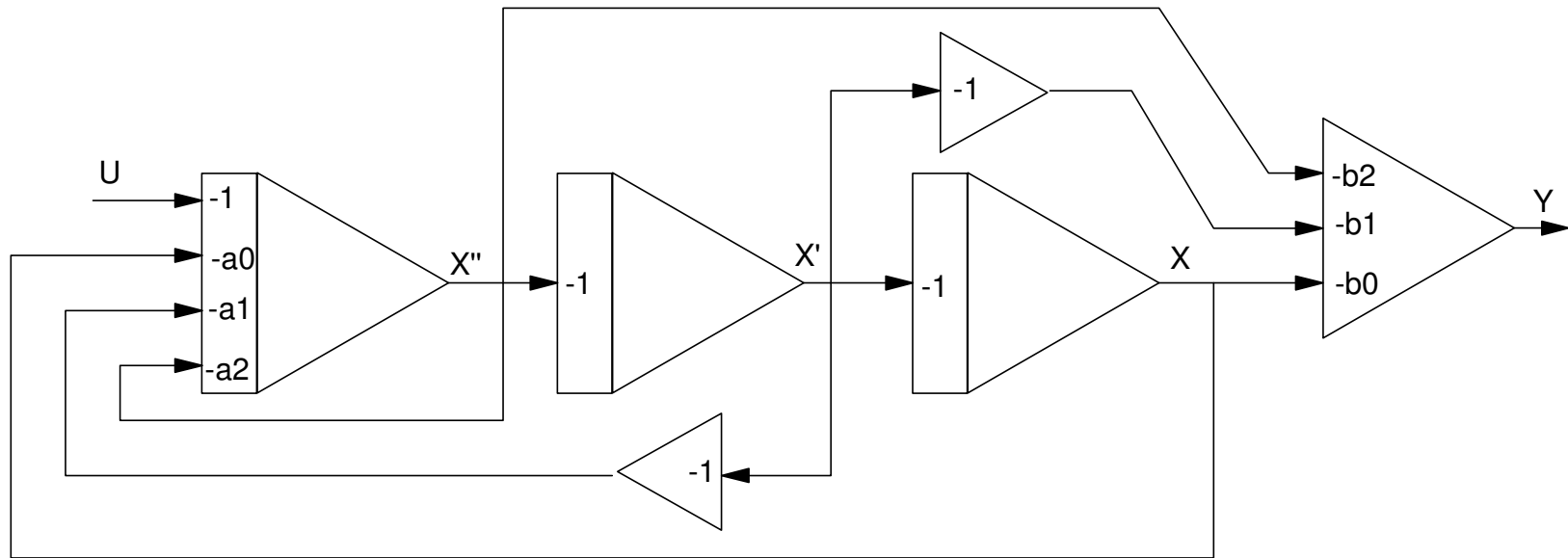
$$Y = (1/s) (-3A - 4B)$$

Applying this to the above block diagram:

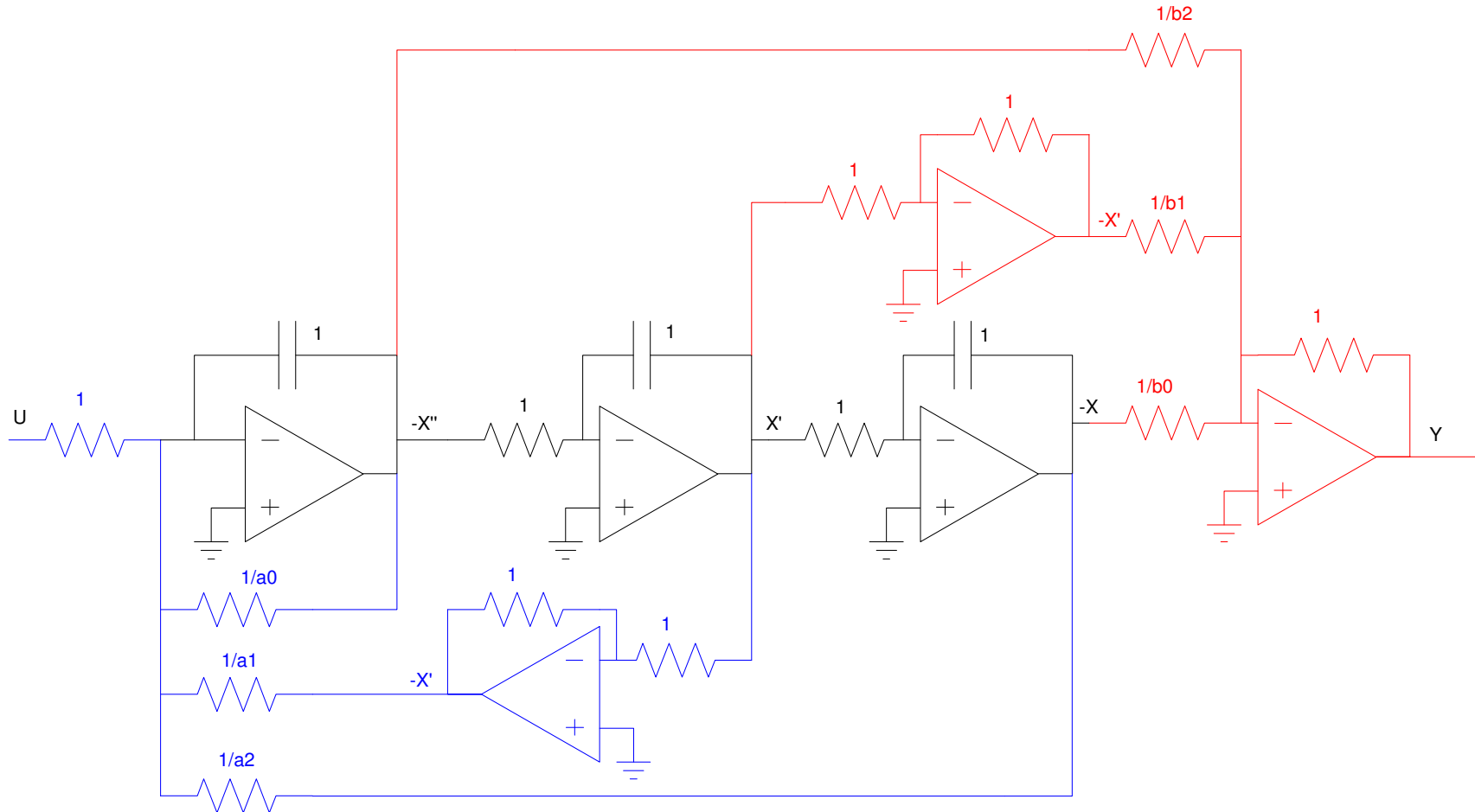


Make all gains negative.

- Keep the sign for all paths from U to Y
- Keep the sign for all loops
- You may have to add inverters



Now convert to an op-amp circuit.



Final Op-Amp Circuit: All units M Ohms and μF .

Sidelight

This technique works well if the poles are close to 1.000

If the poles are not close to 1,

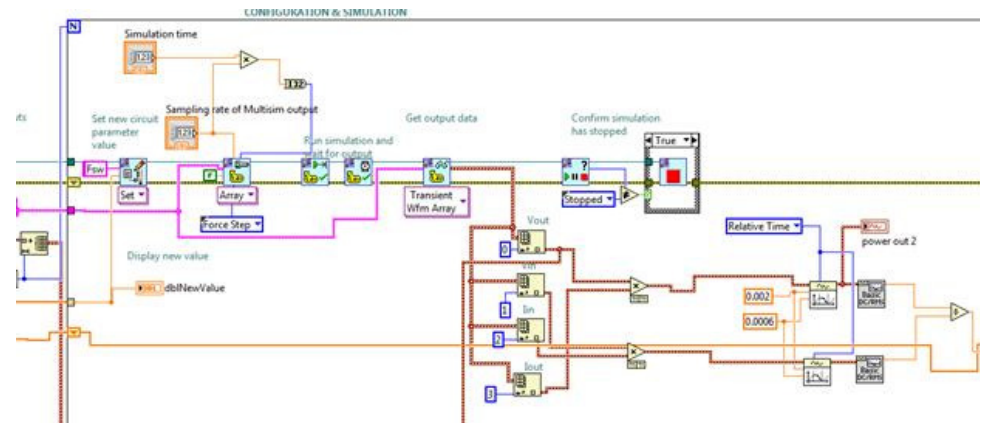
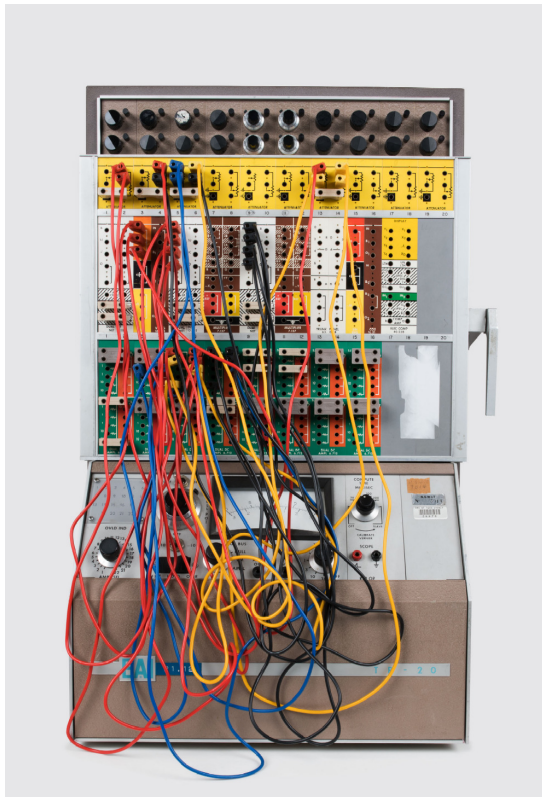
- Scale the poles so that they are close to 1.000
 - Design the analog computer using the previous techniques
 - Scale the circuit by making C larger (slower) or smaller (faster) to return to the original pole locations.
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Modern Analog Computers

Anything you can do in hardware you can do in software

Analog computers are now implemented in software

- LabView, Simulink, VisSim



Summary:

Analog computers are just op-amp circuits

- They allow you to implement any differential equation

The heart is the inverting integrating circuit

- Nth-order differential equation requires N integrators

Plus inverting amplifiers and summing junctions

Somewhat dated:

- You can do the same thing with a microcontroller
- Analog computers are tools: for some applications, they work fine. For others, a microcontroller is easier to use.