

$$\begin{bmatrix} 0 & -1 & 1 & 0 \\ 300 & -200 & 0 & 0 \\ 0 & 0 & -400 & 900 \\ 100 & 300 & 0 & 500 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \\ I_4 \end{bmatrix} = \begin{bmatrix} 0.03 \\ 10 \\ 0 \\ 0 \end{bmatrix}$$

Solve in Matlab

```
-->A = [0,-1,1,0 ; 300,-200,0,0 ; 0,0,-400,900 ; 100,300,0,500]
```

```
0.    - 1.    1.    0.
300.  - 200.  0.    0.
0.    0.    - 400.  900.
100.   300.  0.    500.
```

```
-->B = [0.03;10;0;0]
```

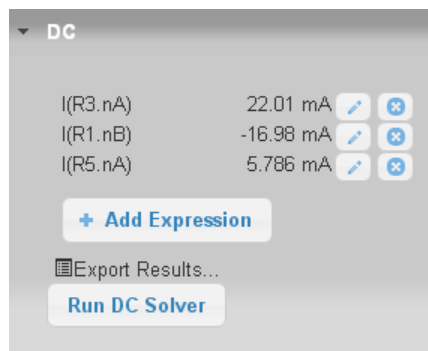
```
0.03
10.
0.
0.
```

```
-->I = inv(A)*B
```

```
I1  0.0220126
I2 -0.0169811
I3  0.0130189
I4  0.0057862
```

c) Check your answers in CircuitLab (or similar circuit simulator)

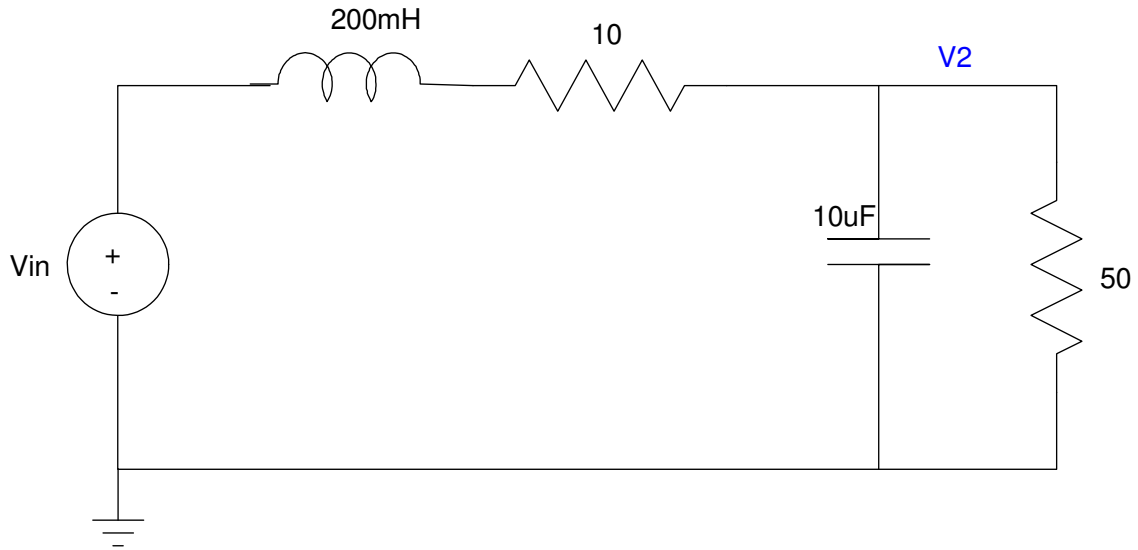
I1, I2, and I4 can be measured directly



5) Assume V_{in} contains a DC and 400 rad/sec (63.66Hz) signal:

$$V_{in} = 10 + 5 \cos(400t) + 6 \sin(400t)$$

a) Determine the voltage, V_2 , using phasor analysis



DC: $V_{in} = 10$

$$s = 0$$

$$V_{in} = 10 + j0$$

$$L \rightarrow j\omega L = 0$$

$$C \rightarrow \frac{1}{j\omega C} = \infty$$

$$V_2 = \left(\frac{50}{50+10} \right) 10 = 8.333V$$

DC term

AC: $V_{in} = 5 \cos(400t) + 6 \sin(400t)$

$$s = j400$$

$$V_{in} \rightarrow 5 - j6$$

$$L \rightarrow j\omega L = j80$$

$$C \rightarrow \frac{1}{j\omega C} = -j250$$

$$50\Omega \parallel -j250\Omega = 48.077 - j9.615\Omega$$

$$V_2 = \left(\frac{48.077 - j9.615}{(48.077 - j9.615) + j(10 + j80)} \right) (5 - j6)$$

$$V_2 = -1.570 - j3.891$$

meaning

$$v_2(t) = -1.570 \cos(400t) + 3.891 \sin(400t)$$

AC term

$$v_2(t) = 8.333 - 1.570 \cos(400t) + 3.891 \sin(400t)$$

total answer: DC + AC

b) Check your answer using CircuitLab (or similar program)

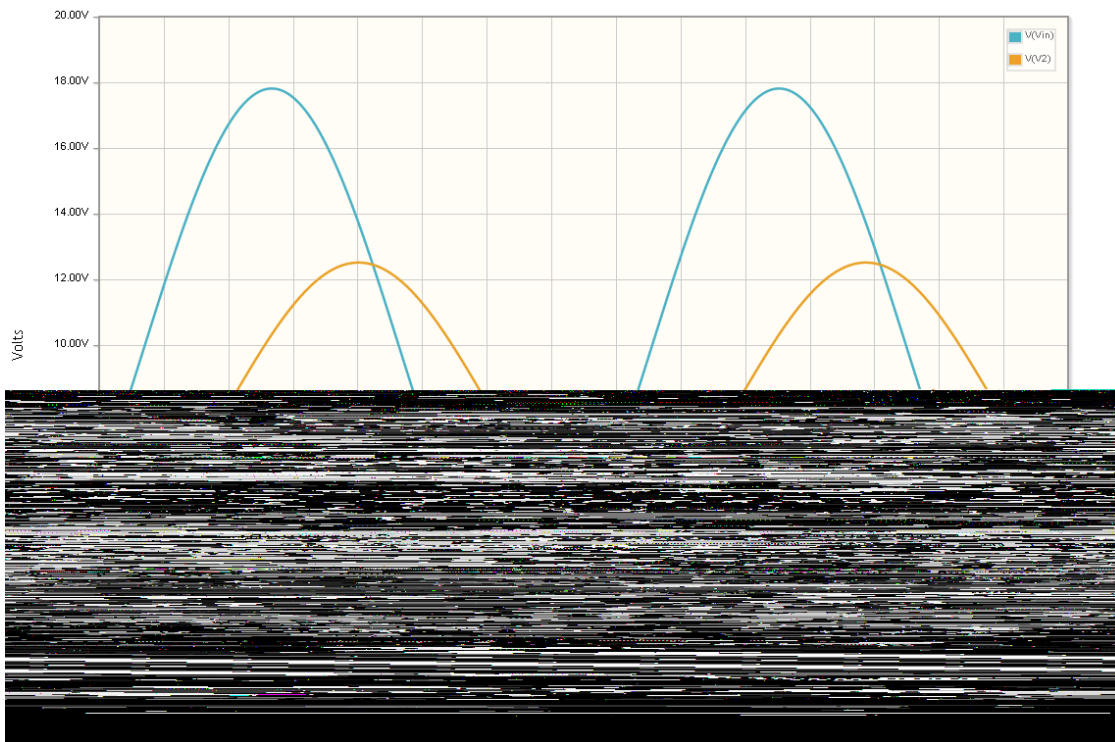
Vin:

$$\omega = 400 = 2\pi f$$

$$f = 63.66\text{Hz}$$

$$V_{in} = 5 - j6 = 7.810 \angle -50.19^\circ$$

The amplitude is 7.81. The phase (sine / cosine relationship) can be accounted for with the phase of Vin. I'll ignore the phase and compute V2 relative to V2



Vor V2 (orange line)

- max = 12.51V
- min = 4.155V

$$V_2 = 8.355V_{pp}$$

From our calculations,

$$V_2 = -1.570 - j3.891 \quad \text{rectangular form}$$

$$V_2 = 4.196 \angle -111.974 \text{ deg} \quad \text{polar form}$$

$$V_{2pp} = 2 * 4.196 = 8.392V_{pp}$$

which matches up with CircuitLab (8.355Vpp)

The phase also matches. The phase of V1 is

$$V_1 = 5 - j6 = 7.810 \angle -50.194^\circ$$

The phase of V2 is

$$V_2 = -1.570 - j3.891 = 4.196 \angle -111.974^\circ$$

V2 lags V1 by 61.78 degrees

From the graph,

The peak of V1 is at 35.40ms

The peak of V2 is at 38.19ms

The period is 15.72ms

V2 lags V1 by

$$\left(\frac{38.19ms - 35.40ms}{15.72ms} \right) 360^\circ = 63.89^\circ$$

which matches our calculations.