







### DC to AC Converter

3) Assume the Fourier transform for the output of a DC to AC converter driving a 1 Ohms resistor is as follows:

- note: units are Vp (peak voltage)

Harmonic	0 (DC)	1	2	3	4	5
an (cosine)	0	18.3	0	2.6	0	0.7
bn (sine)	0	2.7	0	0	1.4	0
Energy (W) $(a_n^2 + b_n^2)/2$	<b>0</b>	<b>171.09</b>	<b>0</b>	<b>3.38</b>	<b>0.98</b>	<b>0.24</b>

Determine the following:

Total Energy in the signal	Energy in the 1st harmonic	Efficiency % of energy in the 1st harmonic
<b>175.69W</b>	<b>171.09W</b>	<b>97.4%</b>

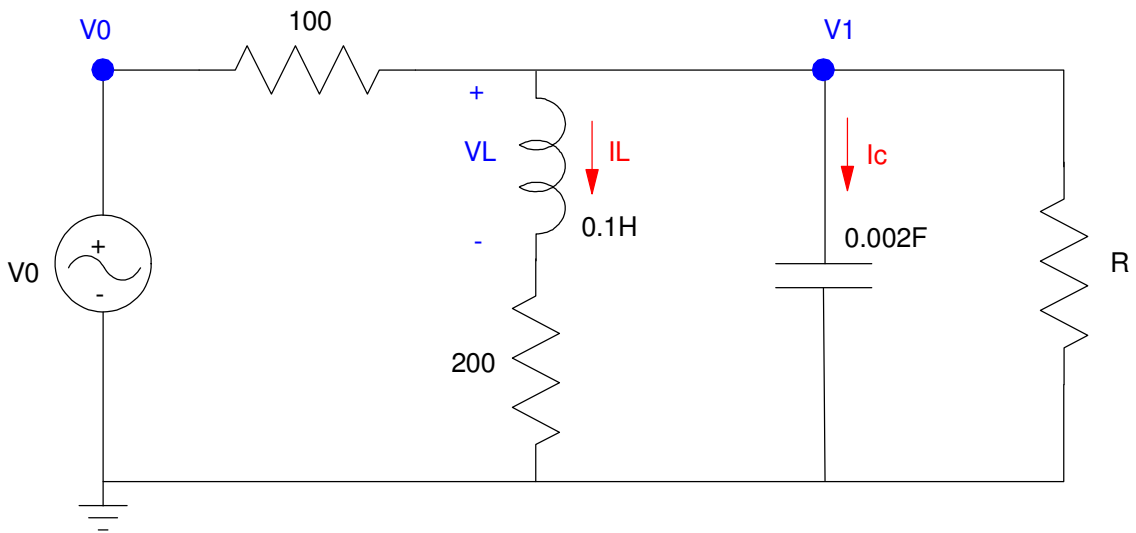
### DC to AC Converter: Differential equations for a Circuit

4) Determine the differential equations which describe the following circuit. Note

- $L = L \frac{I_L}{t}$
- $I = C \frac{1}{t}$

Assume  $R = 1000 + 100 * (\text{Birth Month}) + (\text{Birth day})$ . For May 15th, for example,  $R = 1514$  Ohms.

$\frac{I_L}{t} = 10 \quad 1 - 2000I_L$
$\frac{1}{t} = 5 \quad 0 - 5.33 \quad 1 - 500I_L$



$$L = 0.1 \frac{I_L}{t} = 1 - 200I_L$$

$$\frac{I_L}{t} = 10 \quad 1 - 2000I_L$$

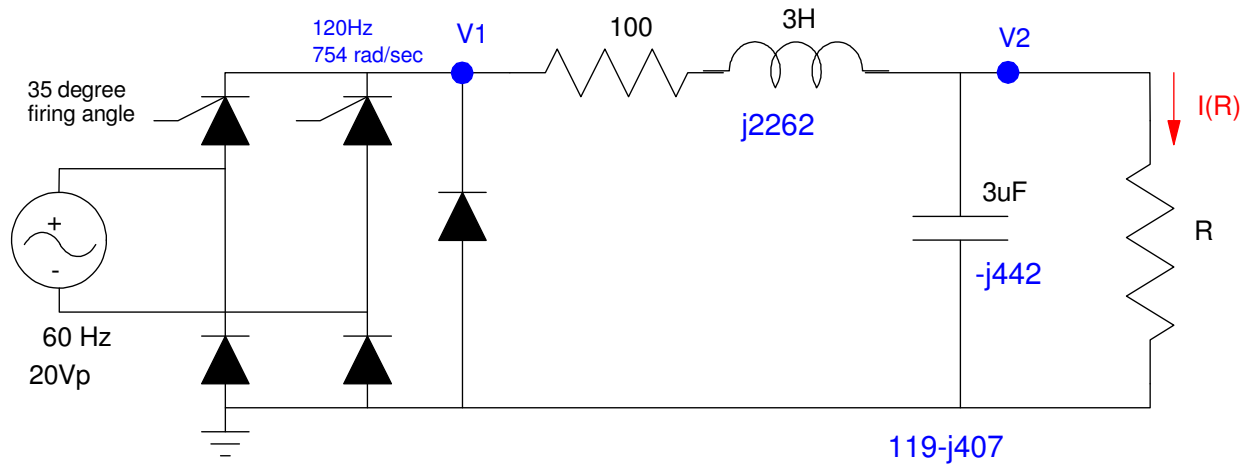
$$0.002 \frac{1}{t} = \frac{0-1}{100} - I_L - \frac{1}{1514}$$

$$\frac{1}{t} = 5 \quad 0 - 5 \quad 1 - 500I_L - 0.33 \quad 1$$

### SCR (5 diode version)

5) SCR: Analysis. Determine the voltages at V1 and V2 (both DC). Assume a firing angle of 35 degrees.

R 1000 + 100*Mo + Day	V1		V2	
	DC	AC (V1pp)	DC	AC (V2pp)
<b>1514</b>	<b>10.48</b>	<b>19.3Vpp</b>	<b>9.83</b>	<b>4.39Vpp</b>



### 35 degrees

$$1(DC) = \frac{18.6 + 0.7}{\pi} (1 + \cos(35^\circ)) - 0.7 = 10.476$$

$$1(AC) = 19.3 \text{ pp}$$

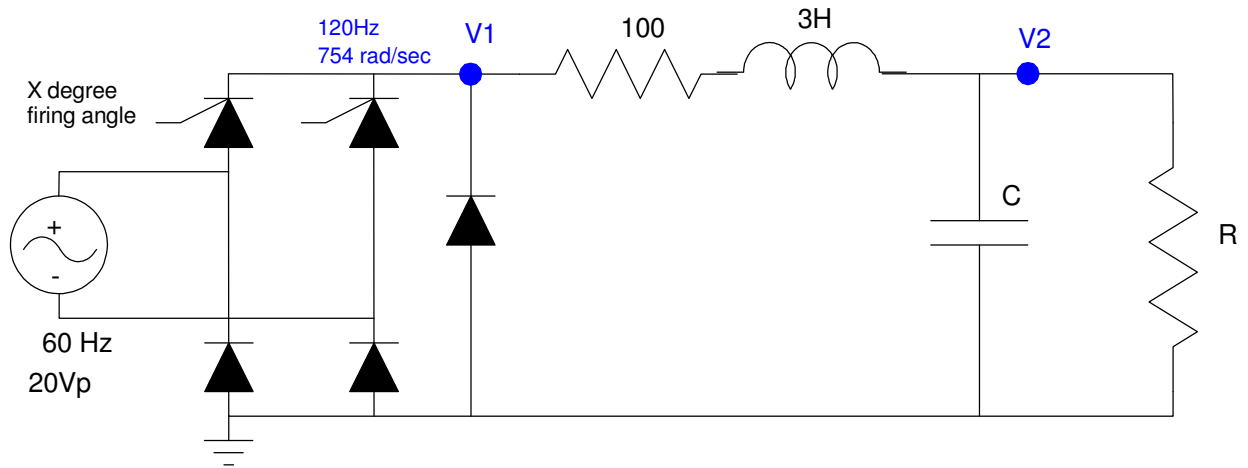
$$2(DC) = \frac{1514}{1514 + 100} 10.476 = 9.827$$

$$2(AC) = \frac{119 - 407}{(119 - 407) + (100 + 2262)} 19.3 \text{ pp} = 4.386 \text{ pp}$$

6) SCR Design. Determine the firing angle and C so that

- $V_2(\text{DC}) = 4.5\text{V}$
- $V_2(\text{AC}) = 500\text{mVpp}$
- $R = 1000 + 100 * (\text{Birth Month}) + (\text{Birth Day})$ . May 14th would give  $R = 1514\ \text{Ohms}$ .

$V_1(\text{DC})$	Firing Angle	C	R $1000 + 100 * \text{Mo} + \text{Day}$
<b>4.797V</b>	<b>96.03 deg</b>	<b>18.1uF</b>	<b>1514</b>



$$V_2 = \frac{1514}{1514+11} \quad V_1 = 4.50$$

$$V_1 = 4.797$$

$$V_1 = 4.797 = \frac{18.6 + 0.7}{\pi} (1 + \cos(\theta)) - 0.7$$

$$\theta = 96.037^\circ$$

$$V_1(\text{AC}) = 18.489 - (-0.7) = 19.189 \text{ pp}$$

If  $C = 0$

$$V_2(\text{AC}) = \frac{1514}{1514+(100+2262)} 19.189 \text{ pp} = 10.373$$

to bring the ripple down to  $0.5\text{Vpp}$

$$\left| \frac{1}{\omega C} \right| = \frac{0.5 \text{ pp}}{10.373 \text{ pp}} 1514 \Omega = 72.98 \Omega$$

$$C = 18.1 \mu\text{F}$$