# Thevenin Equivalent and Load Lines

# EE 206 Circuits I

#### Jake Glower - Lecture #10

Please visit Bison Academy for corresponding lecture notes, homework sets, and solutions

## **Thevenin Equivalent**

So far, we have two tools:

- Voltage Nodes: Find the voltages so that the currents balamoet(szero)
- Current Loops: Find the currents so that the votlages balance to zero)

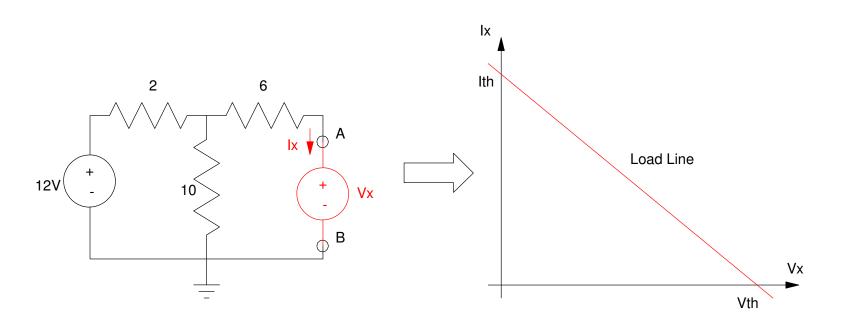
Thevenin Equivalents is tool #3

- Harder to find
- More difficult to comprehend
- Not necessary: you can solve any circuit using current loops datage nodes
- But, Thevenin equivalents can make some circuits much easier to easie

#### Load Lines:

Idea:

- The voltage-current relationship for a linear circuit followstraight line.
- Any circuit which produces the same load line behaves the same
- The simplest circuit which does this is
  - A voltage source & resistor (Thevenin equivalent)
  - A current source & a resistor (Norton equivalent)

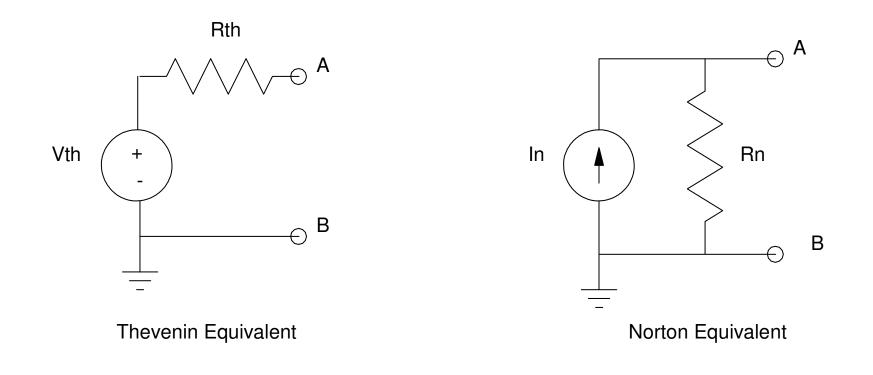


#### **Thevenin and Norton Equivalent**

Simplest circuit to produce a load line

- A voltage source and resistance in series (termed a Thevenin equ); vorten
- A current source and resistance in parallel (termed a Norton ceputi)/el

The trick is to find the values ot Vth, Rth, or Ith



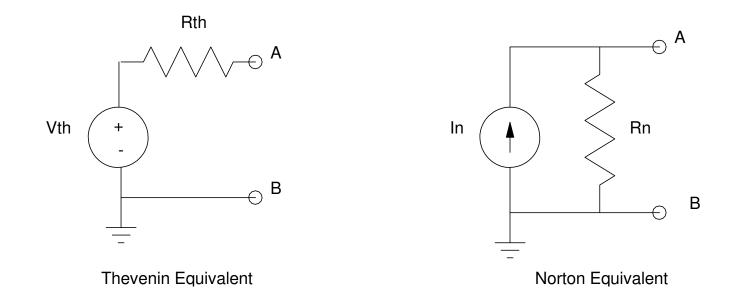
# Finding Vth, Rth, In, Rn

Circuits are equivalent

• Whatever works for your original circuit works for the Tbein / Norton equivalent

Procedure:

- Vth: Measure the open-circuit voltage of your circuit.
- Rth = Rn: Turn off all sources (V = 0, I = 0). Mercesthe resulting resistance.
- In: Measure the short-circcuit current

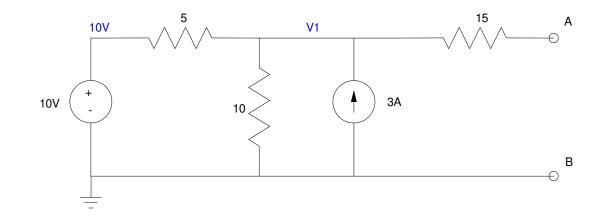


Exa **p** Determine the Thevenin and Norton equivalent ferfollowing circuit:

t Measure the open-circuit voltage.

0

$$\frac{V_{1}-10}{5} + \frac{V_{1}}{10} - 3 = V_{th} = V_{1} = 16.67V$$
  
This is Vth

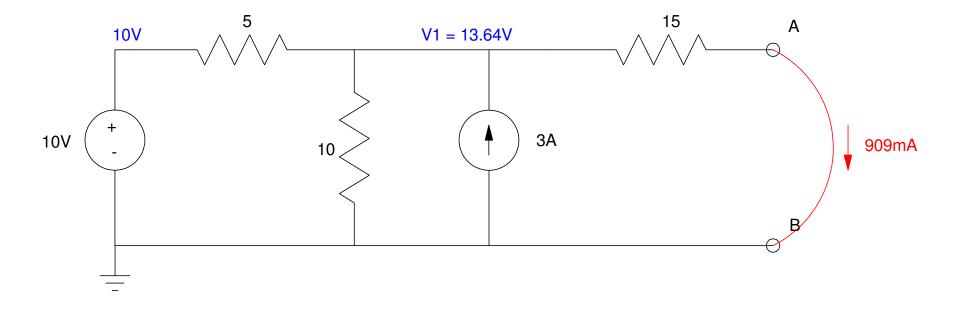


In: Short AB and measure the current. Again, the bolic is so write the node equation at V1

$$\frac{V_1 - 10}{5} + \frac{V_1}{10} - 3 + \frac{V_1}{15} = 0$$

$$V_1 = 13.64V$$

 $I_{\text{short}} = I_{\text{N}} = \frac{13.64\text{V}}{15\Omega} = 909.1\text{mA}$ 

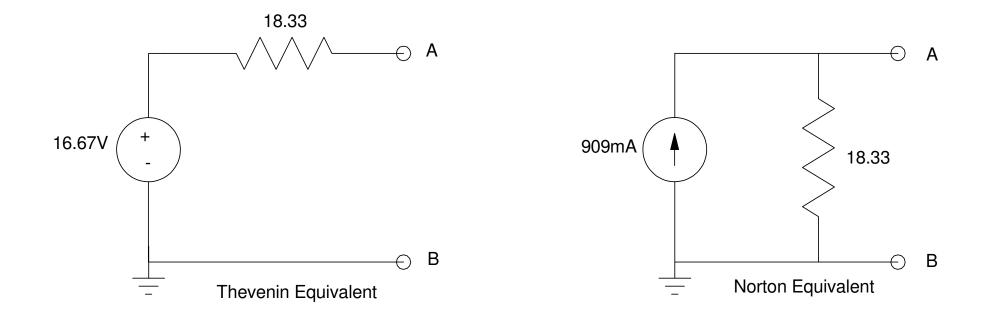


Rth: Turn off the sources (V = 0, I = 0). Meassthe resistance between A and B  $R_{AB} = 15+5||10$  $R_{AB} = 18.333\Omega$ 

Note that you only need to compute two of the set third redundant.

$$R_{AB} = \frac{V_{tn}}{I_n} = \frac{16.67V}{909mA} = 18.33\Omega$$

#### Result:



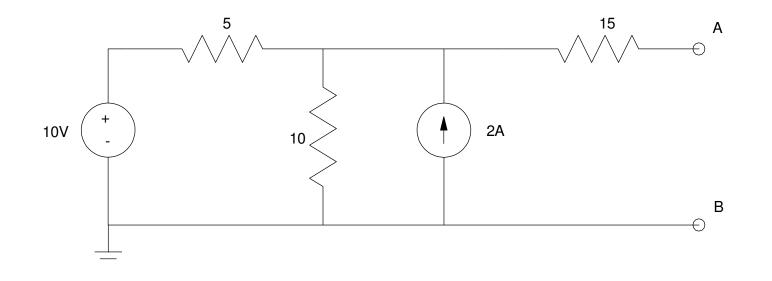
Resulting Thevenin and Norton equivalents of Example 1

## **Circuit Simplification using Thevenin and Norton Equivalent**

Sometimes you can simplify a circuit by flippingtween Thevenin and Norton equivalents

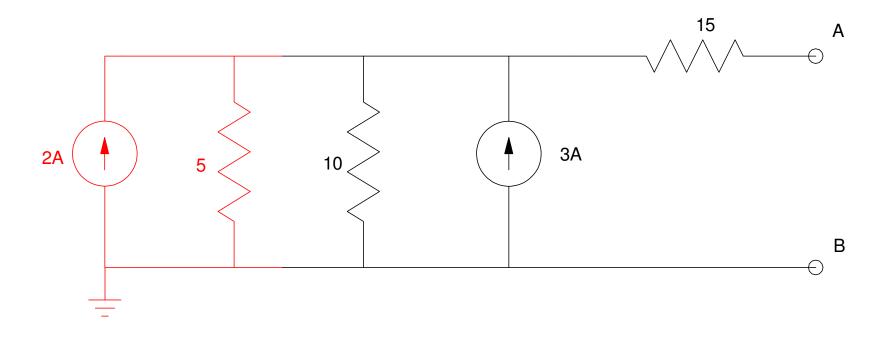
 $R_{\text{Thevenin}} = R_{\text{Norton}}$  $V_{\text{Thevenin}} = I_{\text{Norton}} \cdot R$  $I_{\text{Norton}} = \frac{V_{\text{Thevenin}}}{R}$ 

Eample: Find the Thevenin equivalent



Step 1: Convert the 10V / 5 Ohm resistor to its the equivalent

 $I_{N} = \frac{10V}{5\Omega} = 2A$  $R_{N} = R_{Th} = 5\Omega$ 



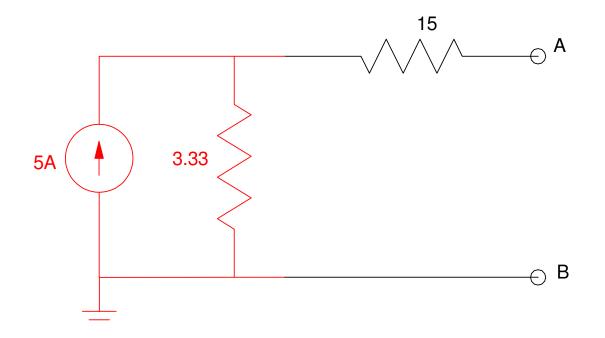
Convert the 10V : 5 Ohm source to its Norton equivalent (shown in red)

Add the resistors in parallel

$$R_{net} = 5||10 = \frac{1}{5} + \frac{1}{10}|^{-1} = 3.333\Omega$$

Add the current soruces

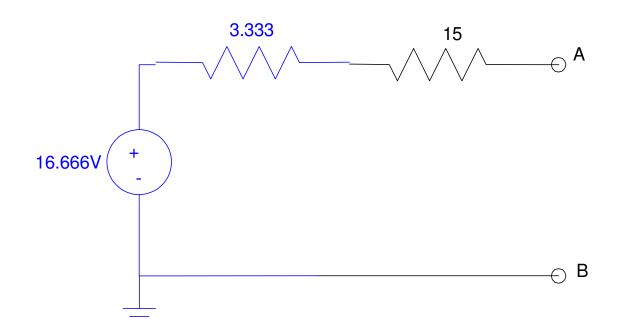
$$I_{net} = 2 + 3 = 5$$



Add the resistors and current sources in parallel:

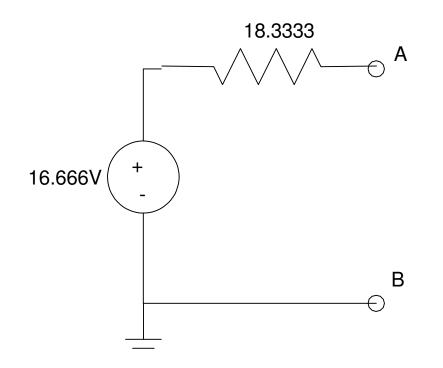
Convert back to a Thevenin equivalent

 $V_{th} = 5A \cdot 3.3333\Omega = 16.666/$ 



Convert to a Thevenin equivalent (shown in blue)

Add the resistors in series and you have the The vequivalent looking in from terminals AB

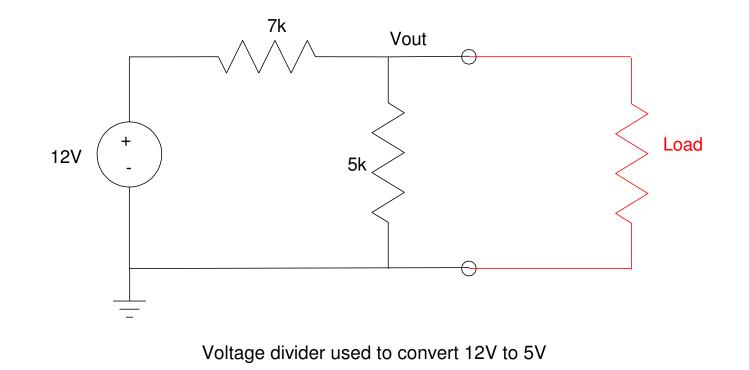


Thevenin Equivalet of Example 2

**Exa p** Thevenin equivalents can provide insight.

• The following voltage divider works (Vout = 5V) if there iso load

When you add a load (100mA @ 5V) the output voltage gozesrto
 Why?

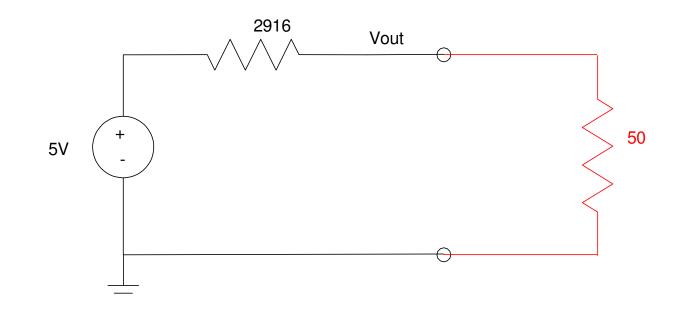


Convert to a Thevenin equivalent

$$V_{th} = V_{open} = \frac{5k}{5k+7k} \quad 12V = 5V$$
  
 $R_{th} = 7k||5k = 2916\Omega$ 

If your load draws 100mA @ 5V, it looks like a 50 10 resistor

 $R_{load} = \frac{5V}{100mA} = 50\Omega$ 



By voltage division, Vout is now

$$V_{out} = \frac{50}{50+2916} \cdot 5V$$
  
 $V_{out} = 0.0843/$ 

This circuit works as a 5V source as long as you't dose it. In Electronics, we'll cover other circuits whice work.

