Thevenin Equivalent and Load Lines

Sofar were looked at two matheds to solve a circuit: arrent these techniques

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Te ida blind Teerineqi valets is that the voltage-arrent r Likewise, any circat vkich has the the same voltage-arrent relation

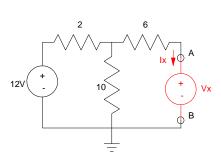
For example, consider the following circuit:

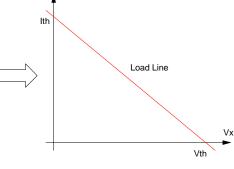
loops and voltage nodes. You can solve any circuit using

dy-bt it can ale some circuits alt easier to analyze if you

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datioship for a liner circuit follow a straigt line sip will betwee excelly the same



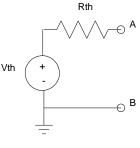


Snee its a liner drait, the VI relationship at the load (V as the load is commend, any drait with the same load line is i

Sne all circuits with the same load line are indistinguishede,

- Avdtage source and resistance in series (termed a Teverin equivelen
- Aarret sorce adresistance in parallel (termela Notonequ'el

The trick is to find the values of Veh, Reh, or Ith

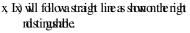


Thevenin Equivalent

Note that these circuits are equivalent to the circuit your early is circuits, you shald get the same result. This leads to the equivalents

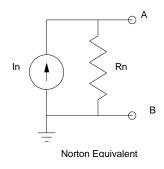
- Vh Natsure the open circuit voltage of your circuit.
- Rh=Ra Timoff all sources (V=0, I=0). Natisu
- In Nature the stort-arcait arrest

It s probably easiest to illustrate this through easies



let suse the similest one possible

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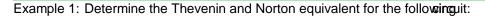


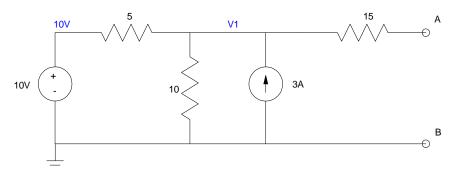
ng Tis news that if you of the same thing to both following procedure to find the Texarin and Noton

re the resulting resistance.

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Exampl e 1: To find V(thevenin), compute the open-circuit voltage

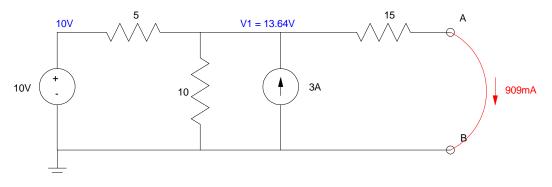
Vth: Measure the open-circuit voltage.

This isn't obvious so let's write the voltage node equation

$$\frac{V_{1}-10}{5} + \frac{V_{1}}{10} - 3 = 0$$
$$V_{th} = V_{1} = 16.67V$$

This is Vth

In: Short AB and measure the current. Again, this isn'icouls vso write the node equation at V1



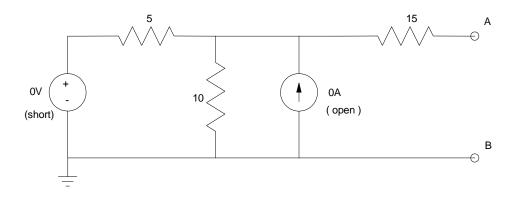
To find I(Norton), short the output and compute the short-circuit current

$$\frac{V_{1} \cdot 10}{5} + \frac{V_{1}}{10} - 3 + \frac{V_{1}}{15} = 0$$

$$V_1 = 13.64V$$

 $I_{short} = I_N = \frac{13.64V}{15W} = 909.1 \text{mA}$

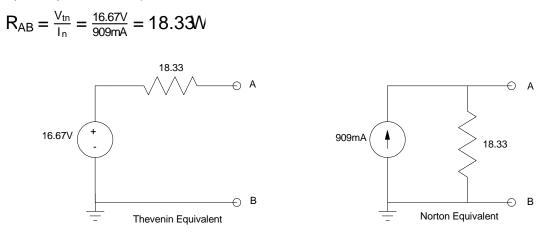
Rth: Turn off the sources (V = 0, I = 0). Measure this tarsce between A and B



To measure the Thevenin resistance, turn off all sources and compute the resistance between A and B

The resistance is

Note that you only need to compute two of these: the their dindant.



Resulting Thevenin and Norton equivalents of Example 1

Circuit Simplification using Thevenin and Norton Eq

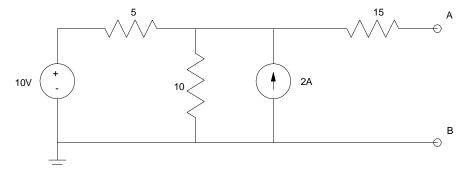
Givena circuit, you can dauge between Teverin and Not on equivalen

ts using the relationship

uivalent

$$\begin{split} R_{\text{Thevenin}} &= R_{\text{Norton}} \\ V_{\text{Thevenin}} &= I_{\text{Norton}} \cdot R \\ I_{\text{Norton}} &= \frac{V_{\text{Thevenin}}}{R} \end{split}$$

For exaple, determe the Treasinequivalent scenar terminal AB

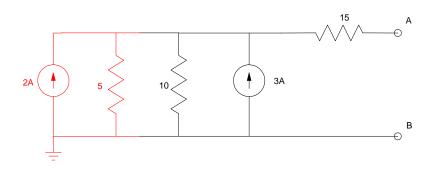


Example 2: Find the Thevenin equivalent at AB

neqivalent

Step 1: Conset the $10\sqrt{7}$ 5 Conversistor to its Noto

$$I_{N} = \frac{10V}{5\Omega} = 2A$$
$$R_{N} = R_{Th} = 5\Omega$$



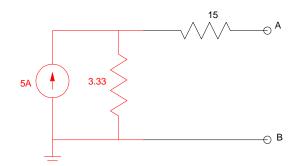
Convert the 10V : 5 Ohm source to its Norton equivalent (shown in red)

Add the resistors in parallel

$$R_{\text{net}} = 5 || 10 = \frac{1}{5} + \frac{1}{10} = 3333 \quad \Omega$$

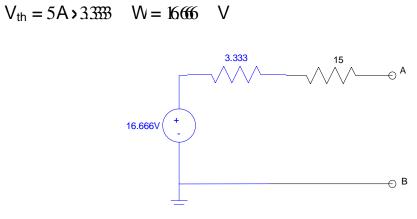
Add the arrest sources

$$I_{net} = 2 + 3 = 5$$



Add the resistors and current sources in paraleel:

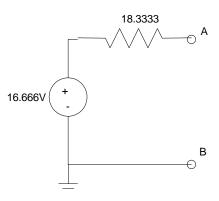
Conert backtoa Teverineqivalert



Convert to a Thevenin equivalent (shown in blue)

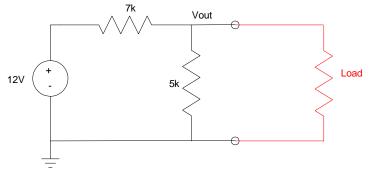
Add the resistors inseries and you have the Teverinequ'valent

locking infrontermals AB



Thevenin Equivalet of Example 2

Example 3: Thevenin equivalents can sometimes provide insight as to other thing doesn't work. For example, the following circuit will convert 12VDC to 5VDC:



Voltage divider used to convert 12V to 5V

If you build this circuit and test it without a loadwiorks: Vout = 5V. If you then connect it to your iPodott dissappears. Why?

To explain that, think Thevenin equivalents. If you conthert to its Thevenin equivalent, you vet

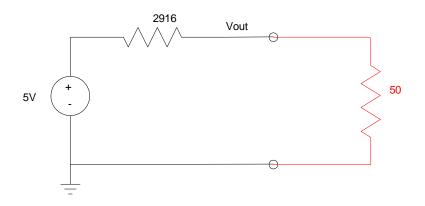
$$V_{th} = V_{open} = \frac{5k}{5k+7k} \quad 12V = 5V$$

$$R_{th} = 7k||5k = 2916W$$

If your load draws 100mA @ 5V, it looks like a 50 Ohesistor

$$R_{load} = \frac{5V}{100mA} = 50W$$

The circuit them becomes



Thevenin eqivalent of the voltage divider driving a load which draws 100mA @ 5V (i.e. a 50 Ohm resistor)

By voltage division, Vout is now

$$V_{out} = \frac{50}{50+2916} \times 5V$$

$$V_{out} = 0.0843/$$

This circuit works as a 5V source as long as you don'ttushe Electronics, we'll cover other circuits which work.