

# ECE 111 - Homework #12

Complex Numbers - Due Monday, April 8th

## Complex Numbers

1) Determine the rectangular or polar form of each complex number

- $3 - j6$
- $-7 - j2$
- $8 \angle 147^\circ$
- $12 \angle -85^\circ$

2) Determine  $y$  as a complex number

- $y = (6 + j8) + (-7 + j8) + (3 - j7)$
- $y = (4 \angle 84^\circ) + (7 \angle -62^\circ) + (9 \angle 85^\circ)$

3) Determine  $y$  as a complex number

- $y = \left( \frac{(6+j8)(-7+j8)}{(3-j7)} \right)$
- $y = \left( \left( \frac{6+j8}{-7+j8} \right) + \left( \frac{9+j6}{-j7} \right) \right) \left( \frac{-2+j6}{8+j9} \right)$

4) Determine  $y$  as a complex number

- $y = e^{(3+j7)}$
- $y = \ln(-9 + j9)$
- $y = (4 + j5)^{(5-j2)}$

## Partial Fractions with Complex Numbers

5) Determine the partial fraction expansion

$$\left( \frac{3(x-7)(x+4)}{(x+9+j4)(x+9-j4)(x+9)} \right) = \left( \frac{a}{x+9+j4} \right) + \left( \frac{b}{x+9-j4} \right) + \left( \frac{c}{x+9} \right)$$

6) Determine the partial fraction expansion

$$\left( \frac{8(x+j6)(x-j6)}{x(x+4)(x+9+j)(x+9-j)} \right) = \left( \frac{a}{x+0} \right) + \left( \frac{b}{x+4} \right) + \left( \frac{c}{x+9+j} \right) + \left( \frac{d}{x+9-j} \right)$$